

# Development of film thickness in elastohydrodynamically lubricated compliant contacts

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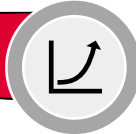
INSTITUTE OF MACHINE  
AND INDUSTRIAL DESIGN

# CONTENT

- Motivation
- Introduction
  - State of the art
    - Literature review
      - Aim of thesis
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    - Materials and methods
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- Conclusion

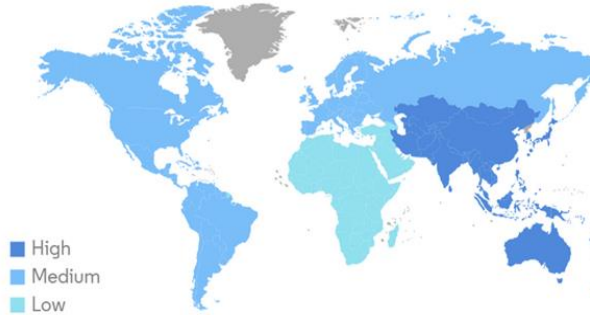
# MOTIVATION

## Commercial



- Expansion of polymer gears in mechanical engineering

Growth Rate by Region, 2023 – 2028



Source: Mordor Intelligence

Plastic gearbox market, Mordor intelligence (2023)

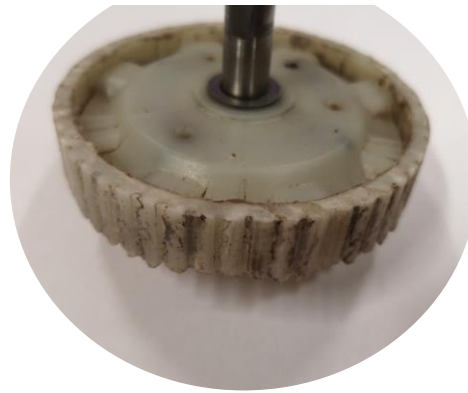


# Perspectives

## Engineering



- Prevention of the failure modes of polymer gears



Failure of polymer gear, Krupka (2019)

## Scientific



- Increase of polymer gears performance under lubricated conditions

EHL

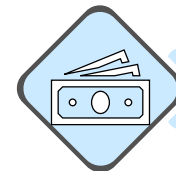


Tribological experiments, Krupka (2019)



## Participation in scientific projects

- Thermo-elasto-hydrodynamics of coated polymer gears (Grant No. 18 – 26849J)



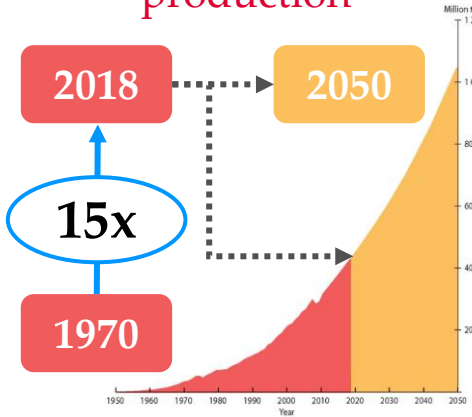
## Project funding



# INTRODUCTION

## Plastics

Grow of plastics production



Plastic products examples



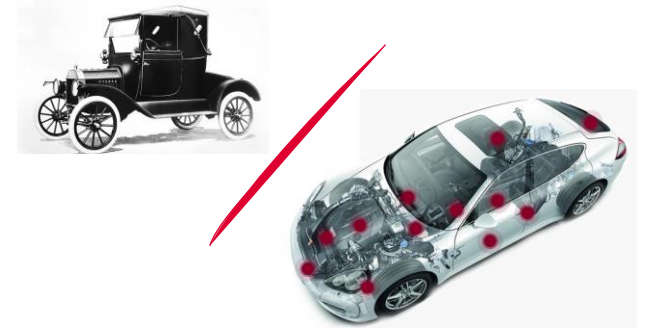
## Polymer machine elements



- Low-cost production
- Low mass
- Ability to damp shocks and vibrations
- Silent operation
- Resistance to oils and acids

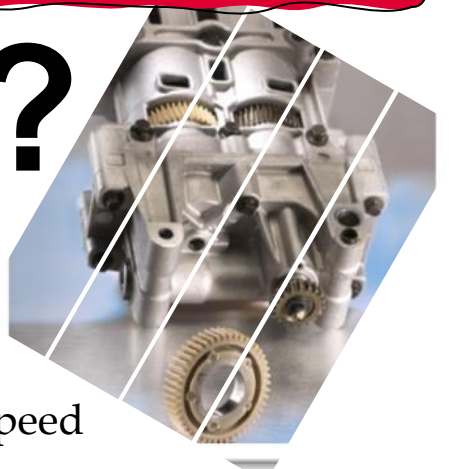
## Applications

- Automotive industry
- Aerospace industry
- Industrial equipment
- Electrical appliances
- Medical industry



## High-performance applications

Transmissions and differentials



High torque

temperature

speed

## Lubrication



Dry conditions



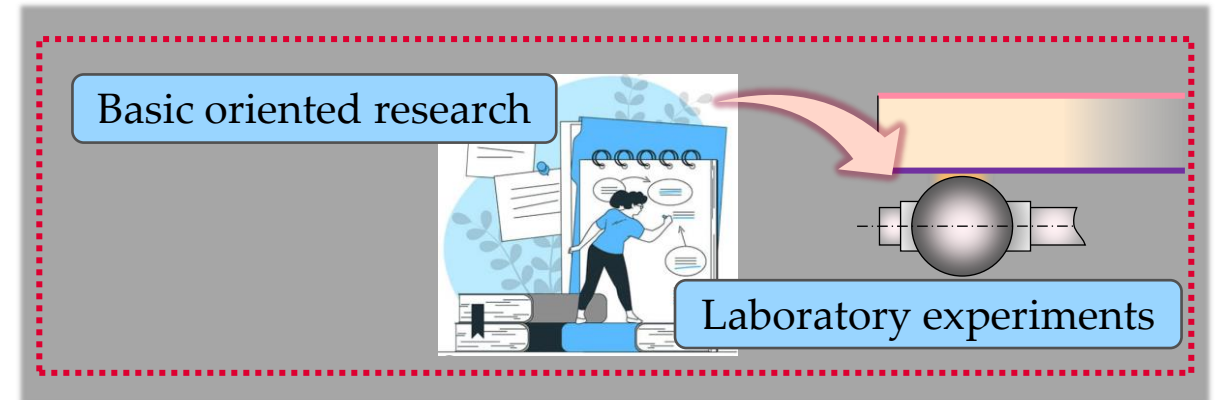
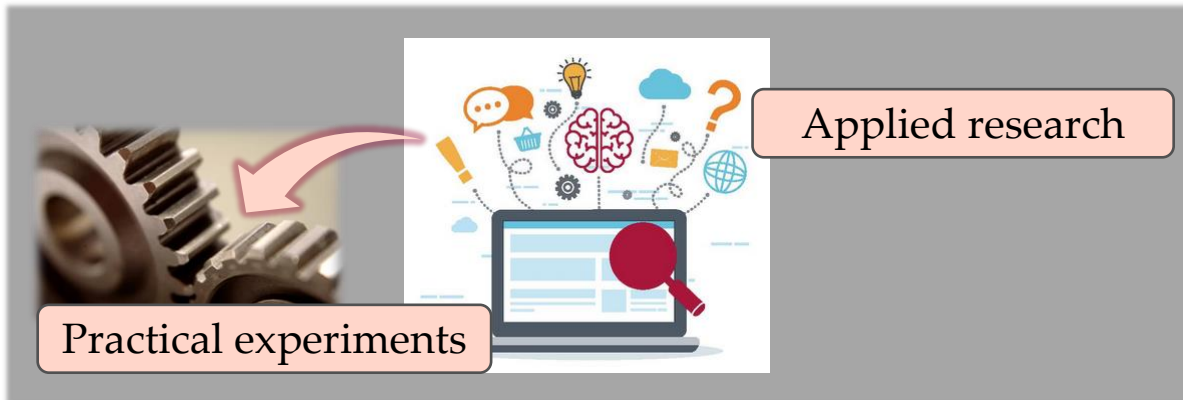
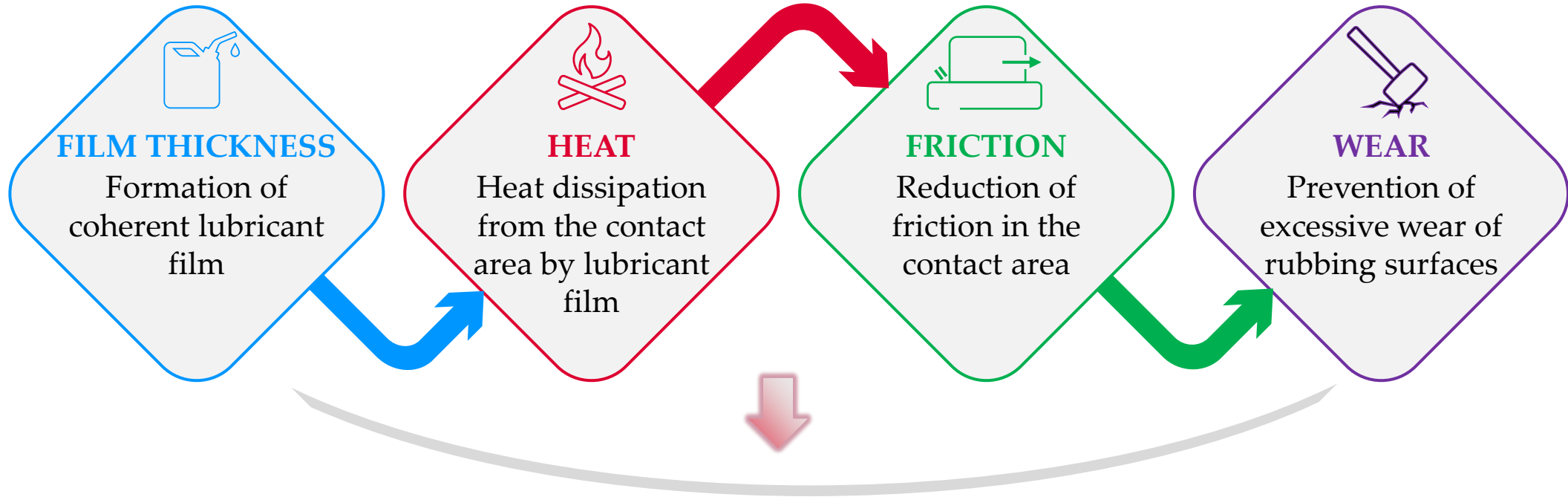
Grease lubrication



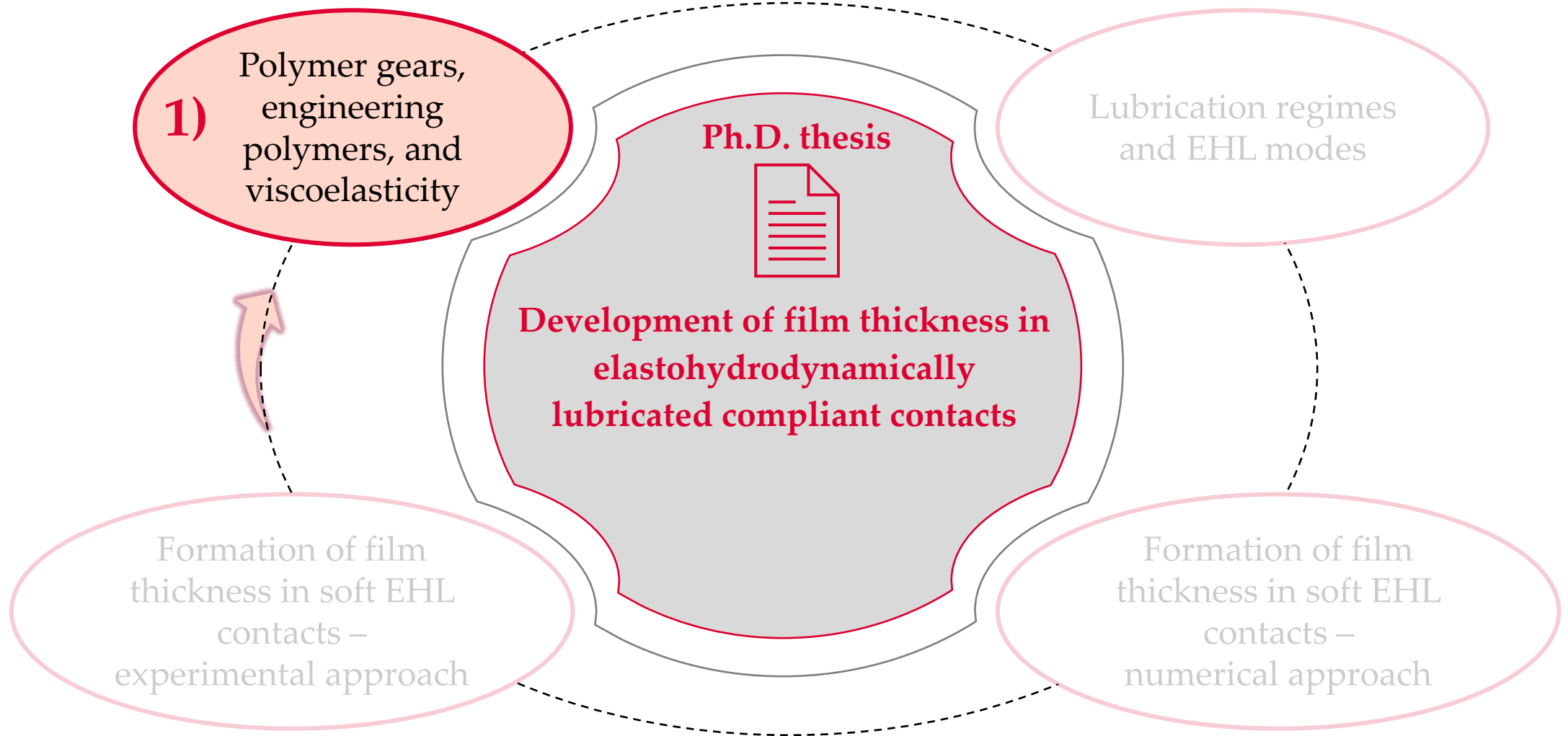
Liquid lubrication

Lubricant film thickness

# INTRODUCTION



# STATE OF THE ART



# STATE OF THE ART

## Polymer gears



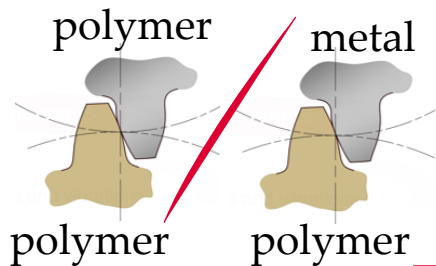
spur

helical

bevel

worm

## Gearsets



Compliant contact

## Failure modes



## Engineering polymers

- PA 66, PEEK, POM

Properties / polymer	PA 66	PEEK	POM	PU	PFTE	100Cr6
Maximal service temperature, $T_s$ (°C)	80	250	85	80	250	-
Glass-transition temperature, $T_g$ (°C)	47	143	-40	-60	-100	-
Thermal conductivity, $\lambda$ (W/m °C)	0.25	0.28	0.27	0.03	0.23	46.6
Thermal expansion, $\beta$ ( $10^{-6}$ °C)	88	55	93	150	145	12
Elastic modulus, E (GPa)	2.50	3.75	2.80	1.85	0.67	210
Yield strength, $R_e$ (MPa)	90	130	80	90	15	700
Poisson's ratio, $\nu$ (-)	0.41	0.40	0.35	0.48	0.46	0.30

## Modification of polymer properties

### Mechanical

Glass fibers (GF)  
Carbon fibers (CF)

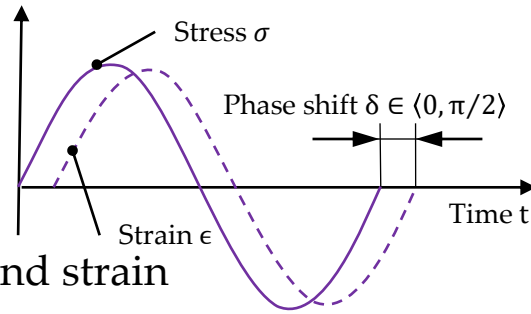
### Tribological

Teflon (PFTE)  
Molybdenum disulfide (MoS<sub>2</sub>)

# STATE OF THE ART

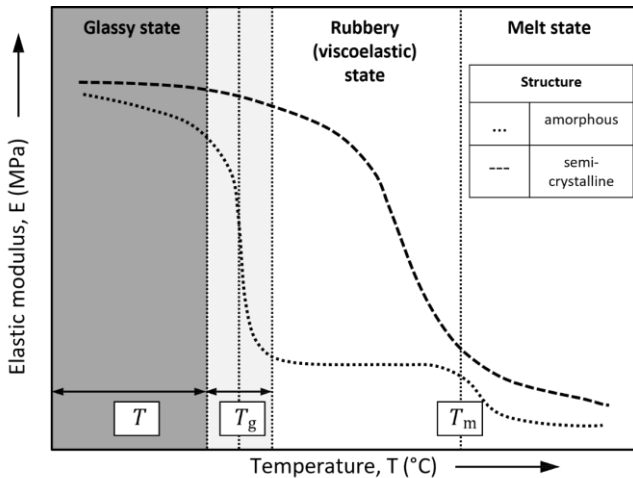
## Viscoelasticity of polymers

- Inelastic response of material
- Time dependence between stress and strain
- Significant temperature dependence
- Glass-transition temperature,  $T_g \rightarrow$



## Polymer states

Elastic modulus vs temperature



Glassy  $\rightarrow T < T_g$

Rubbery  $\rightarrow T \sim T_g$

Melt  $\rightarrow T > T_g$

## Macromolecular arrangement

Amorphous  
(PC, PMMA)

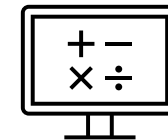
Semi-crystalline  
(PA66, PEEK)

Crystalline



## Determination of viscoelastic response

Numerical simulation

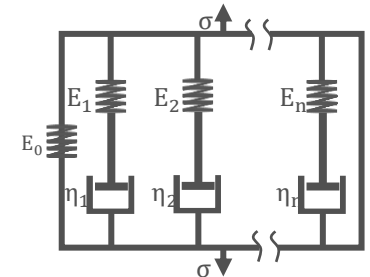


SLS and generalized models

Experiments

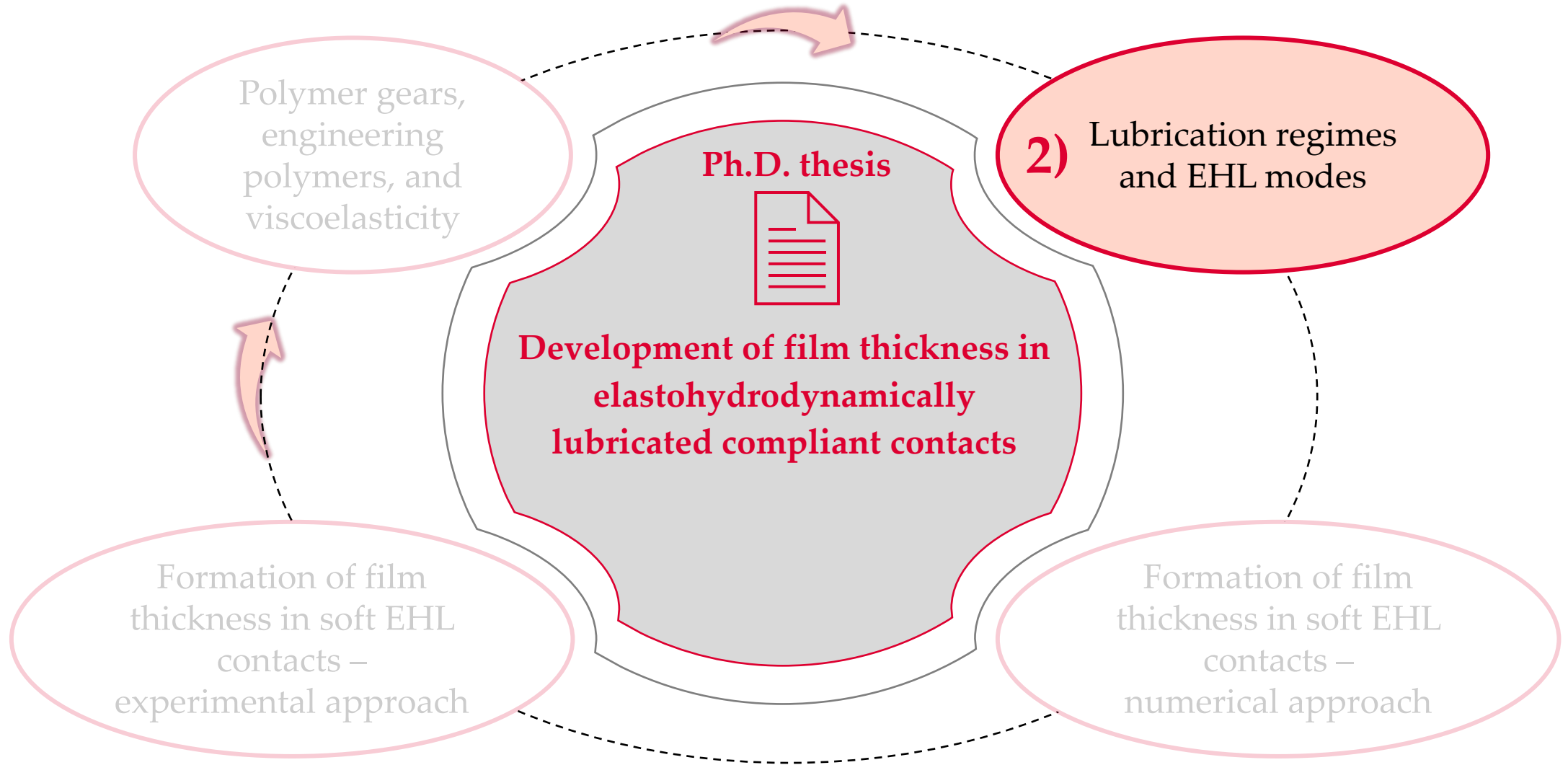


Nano-DMA and DMA



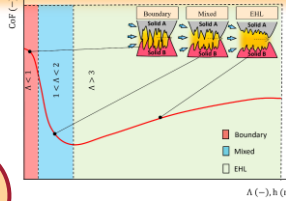


# STATE OF THE ART



# STATE OF THE ART

GRUBIN, A.N., 1949  
BLOK, H., 1959



First findings about (hard) EHL

1950s

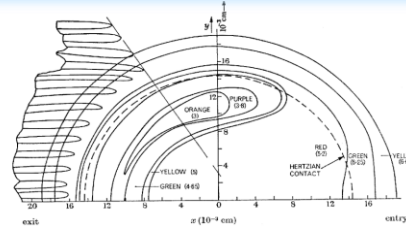
First use of engineering polymers

Intensive research in (hard) EHL

1960s

First use of polymer gears

HOOKE, C. J., 1965  
HERREBRUGH, K., 1966  
DOWSON, D., 1967  
ARCHARD, J. F., 1968



DOWSON, D., 1967



First findings about (soft) EHL

1970s

Growth of polymers in engineering

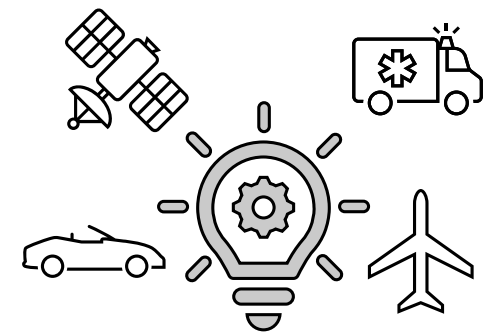
JOHNSON, K. L., 1970



**Definition of EHL modes**

- Piezoviscous-elastic (P-E)
- Piezoviscous-rigid (P-R)
- Isoviscous-elastic (I-E)
- Isoviscous-rigid (I-R)

JOHNSON, K. L., 1970



# STATE OF THE ART

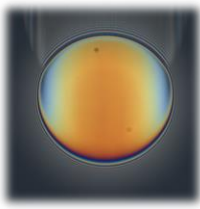
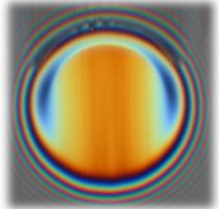
## EHL modes

Piezoviscous-elastic (P-E)

Isoviscous-elastic (I-E)

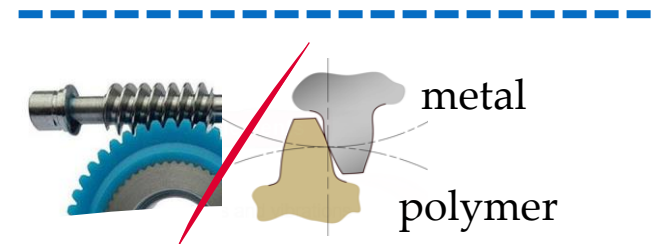
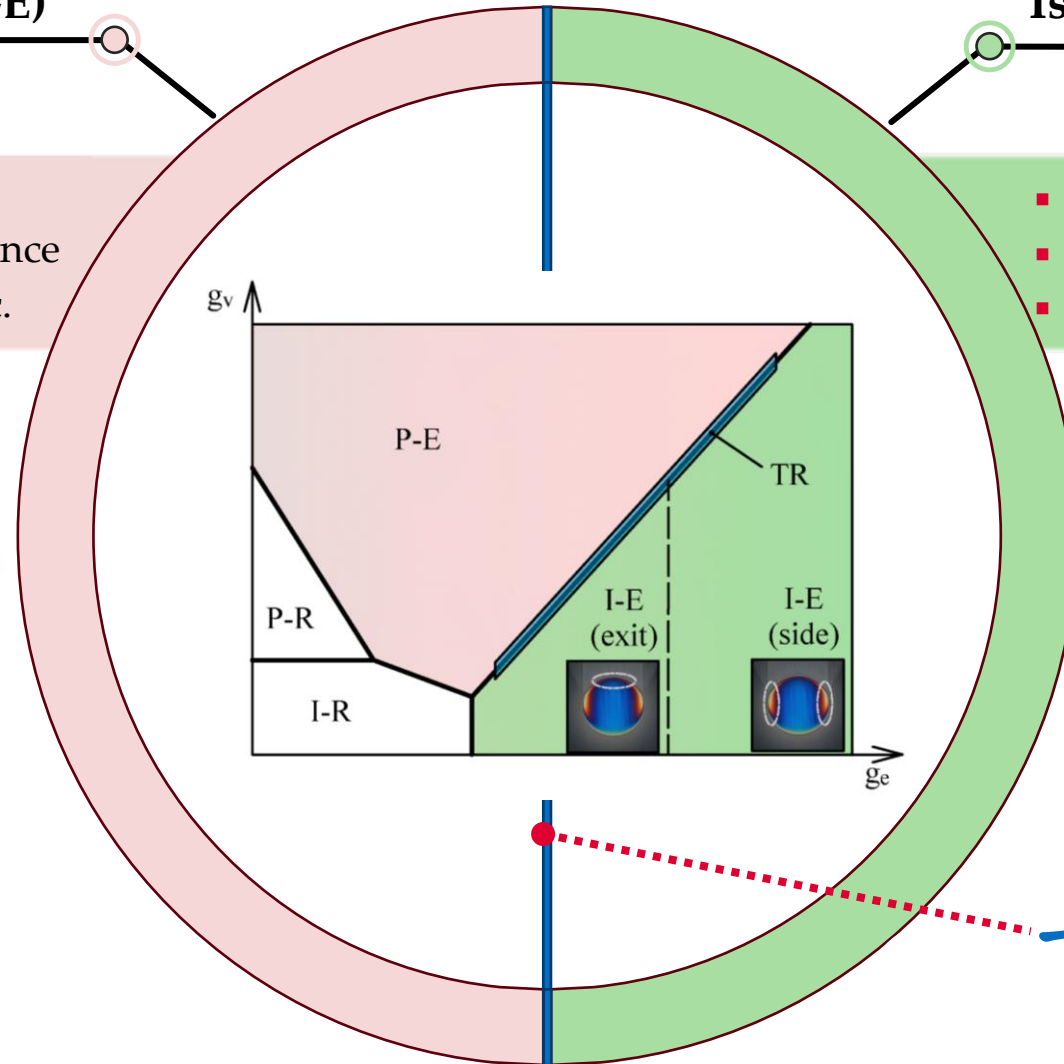
hard EHL

soft EHL



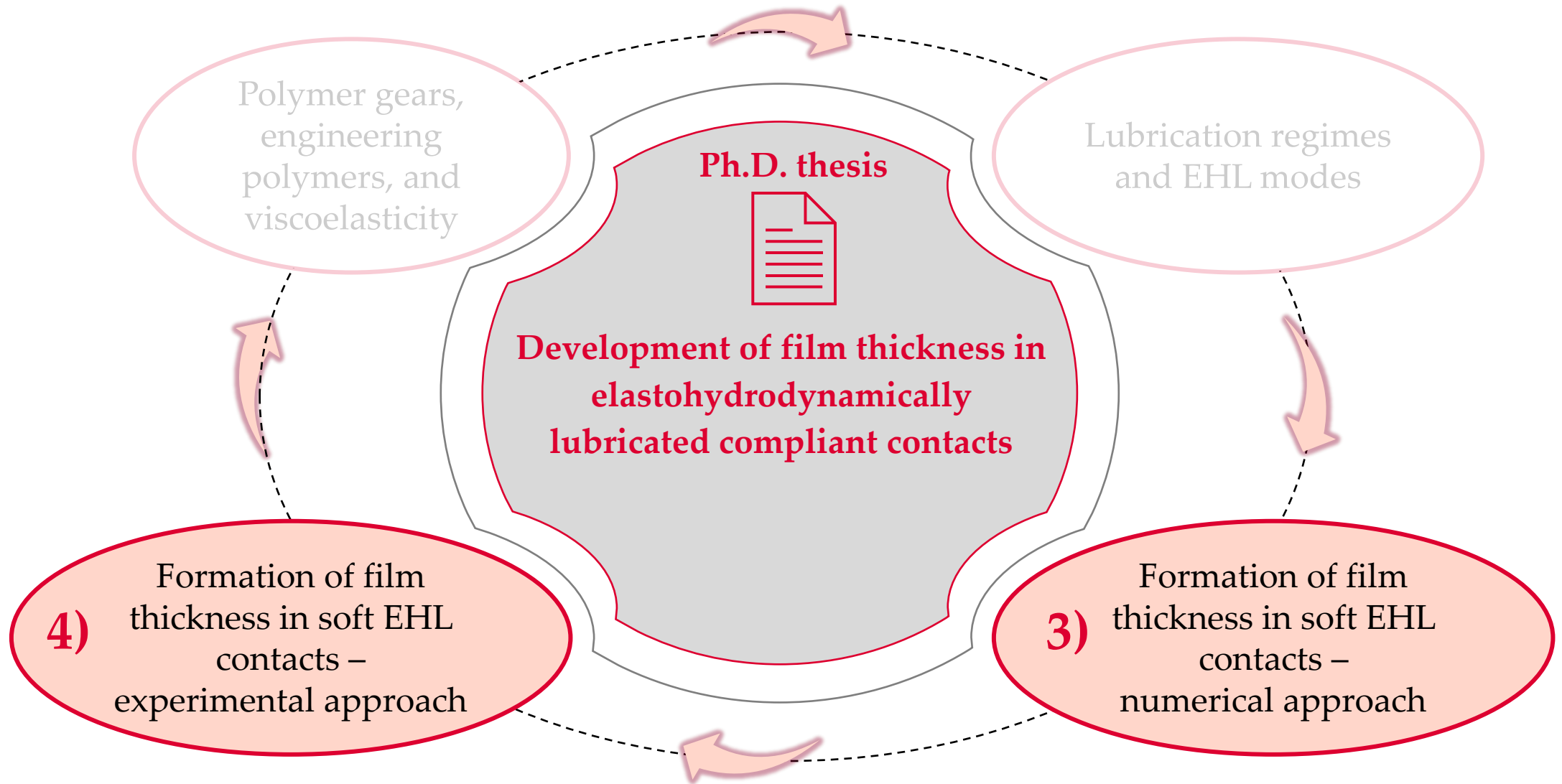
- $p = (0.5 - 4) \text{ GPa}$
- strong  $p-\eta$  dependence
- metals, ceramics etc.

- $p \leq 50 \text{ MPa}$
- weak  $p-\eta$  dependence
- thermoplastics, rubbers etc.



TR region = ?

# STATE OF THE ART



# STATE OF THE ART- analysis of lubricant film in soft EHL

Johnson et al.  
Hooke et al.  
Hamrock et al.

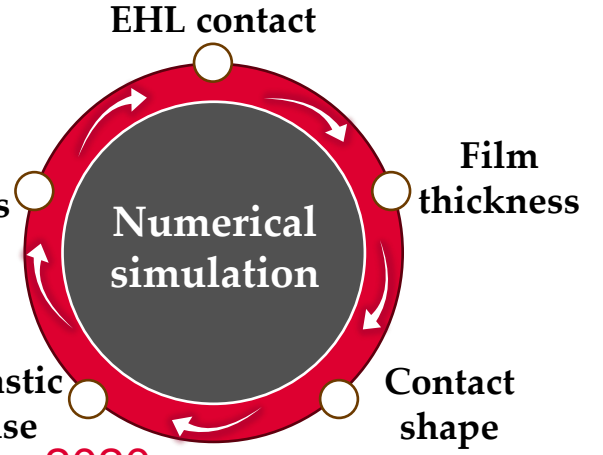
- Circular, elliptical, and disc contacts
- Prediction of magnitude of film thickness
- Definition of parameters  $\bar{U}$  and  $\bar{W}$

Esfahanian et al.

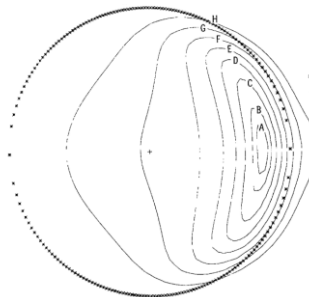
- Revisited EHL maps
- Circular and elliptical contacts

Myant et al.  
Gasni et al.  
Stupkiewicz et al.  
Marx et al.

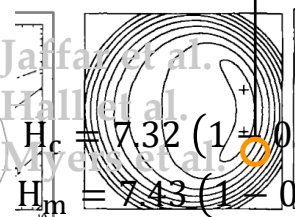
SLS models



1970s



1980s



Exit

Side

$$H_c = 7.32 (1 + 0.72 e^{-0.28k}) \bar{U}^{0.64} \bar{W}^{-0.22}$$

$$H_{im} = 7.43 (1 + 0.85 e^{-0.5k}) \bar{U}^{0.65} \bar{W}^{-0.21}$$

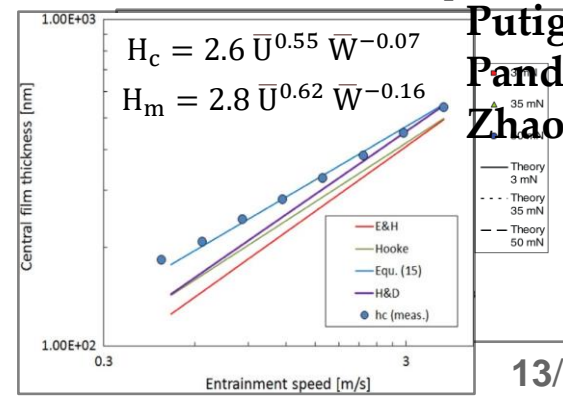
1990s

2000s

Bohan et al.  
Skotheim et al.  
Bongaerts et al.

2010s

- Circular contact (steel/PEEK/PMMA/BK7 disc)
- Effect of  $\bar{U}$ ,  $\bar{W}$ , and SRR
- Chromatic interferometry

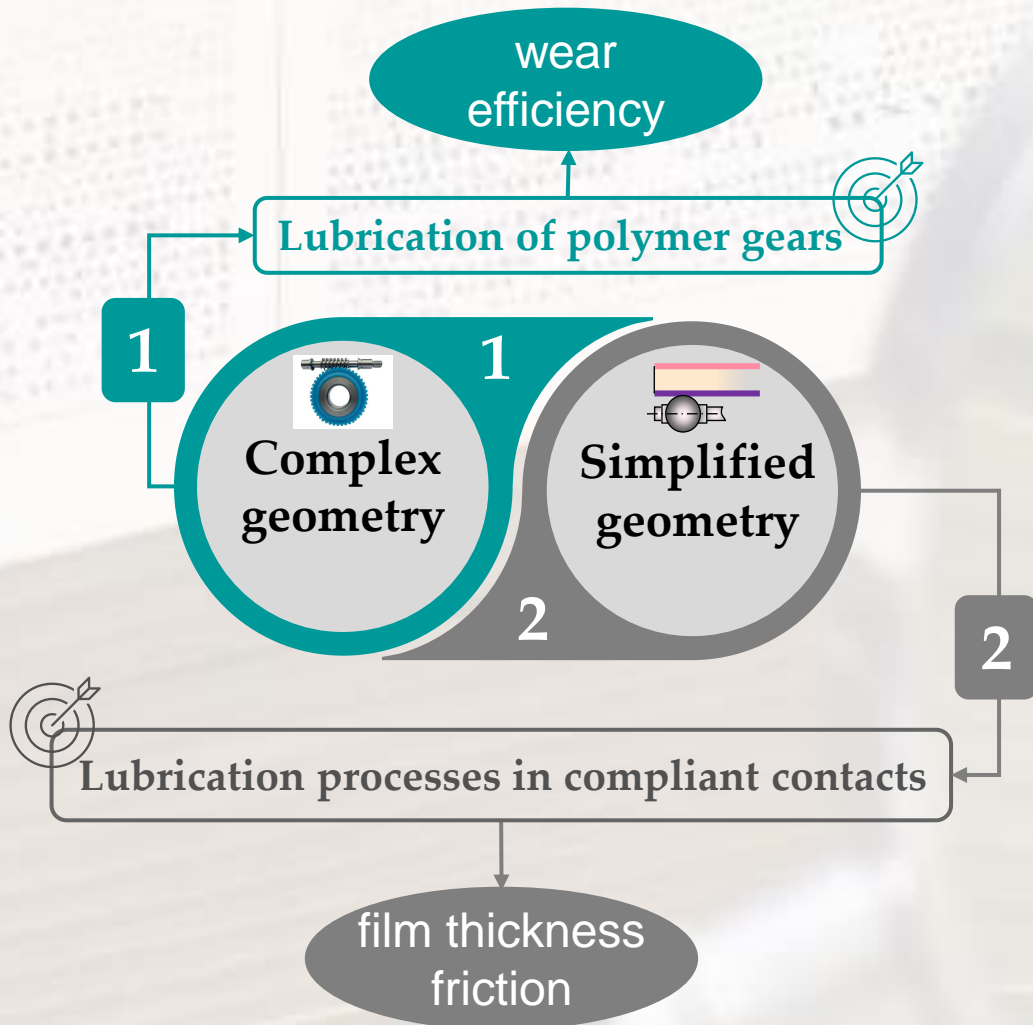


Putignano et al.  
Pandey et al.  
Zhao et al.

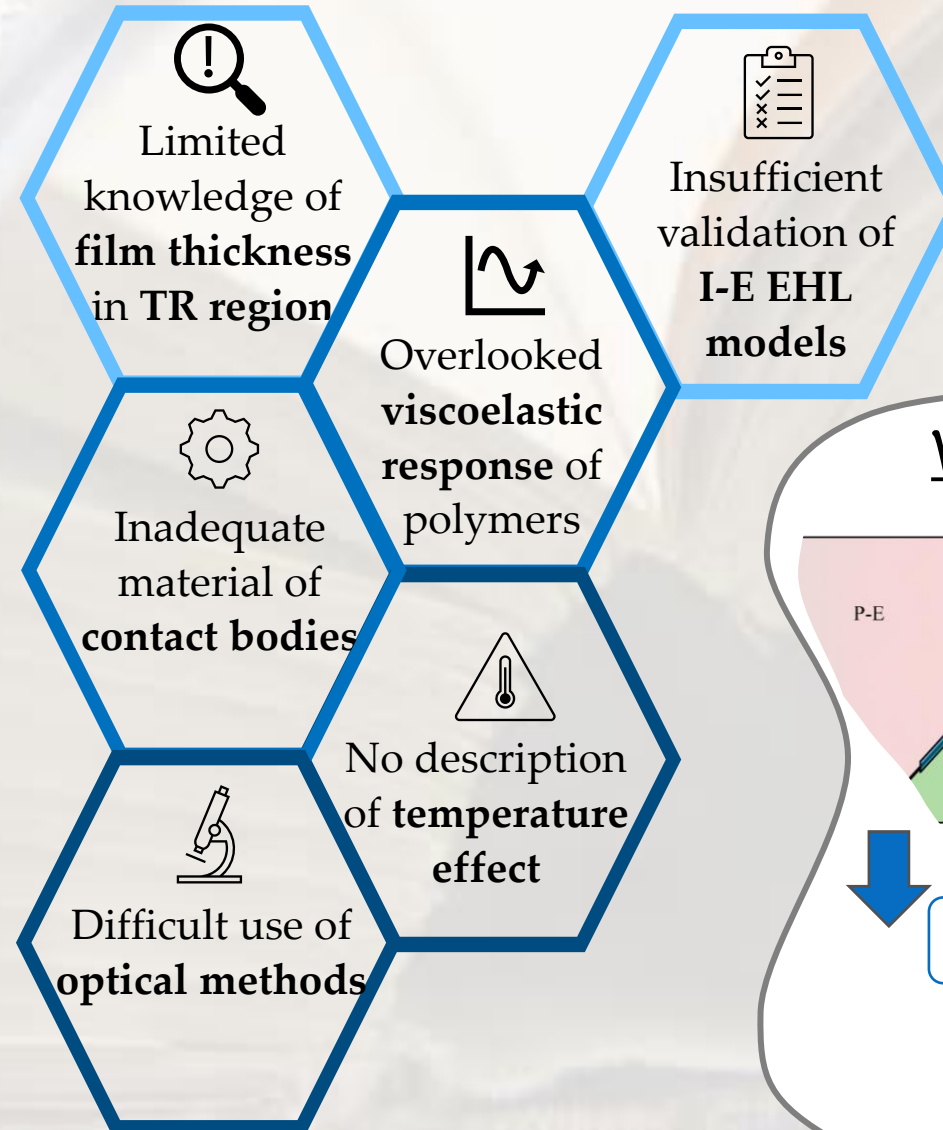
2020s

# SUMMARY OF LITERATURE REVIEW

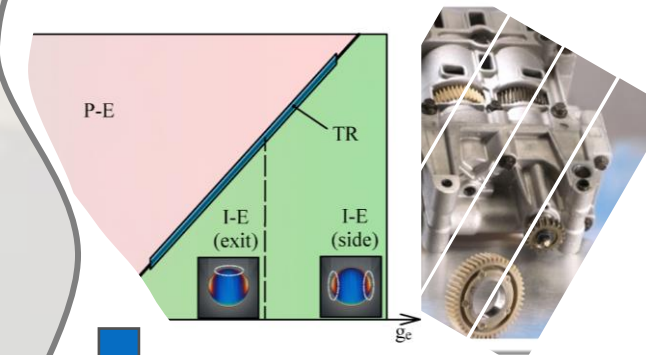
## Compliant contacts



## Shortcomings



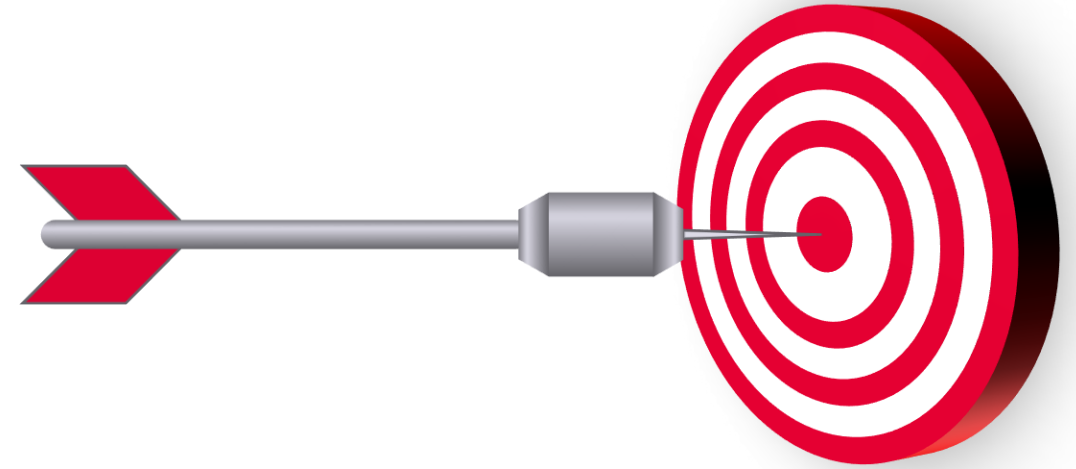
## White space



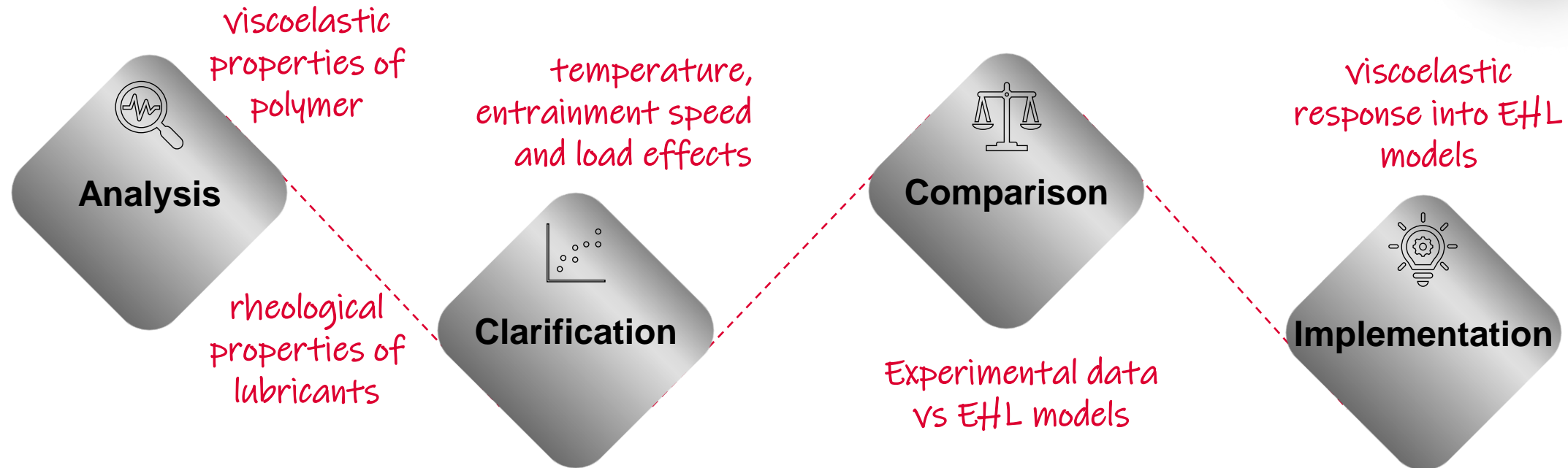
TR region of EHL

# AIM OF THESIS

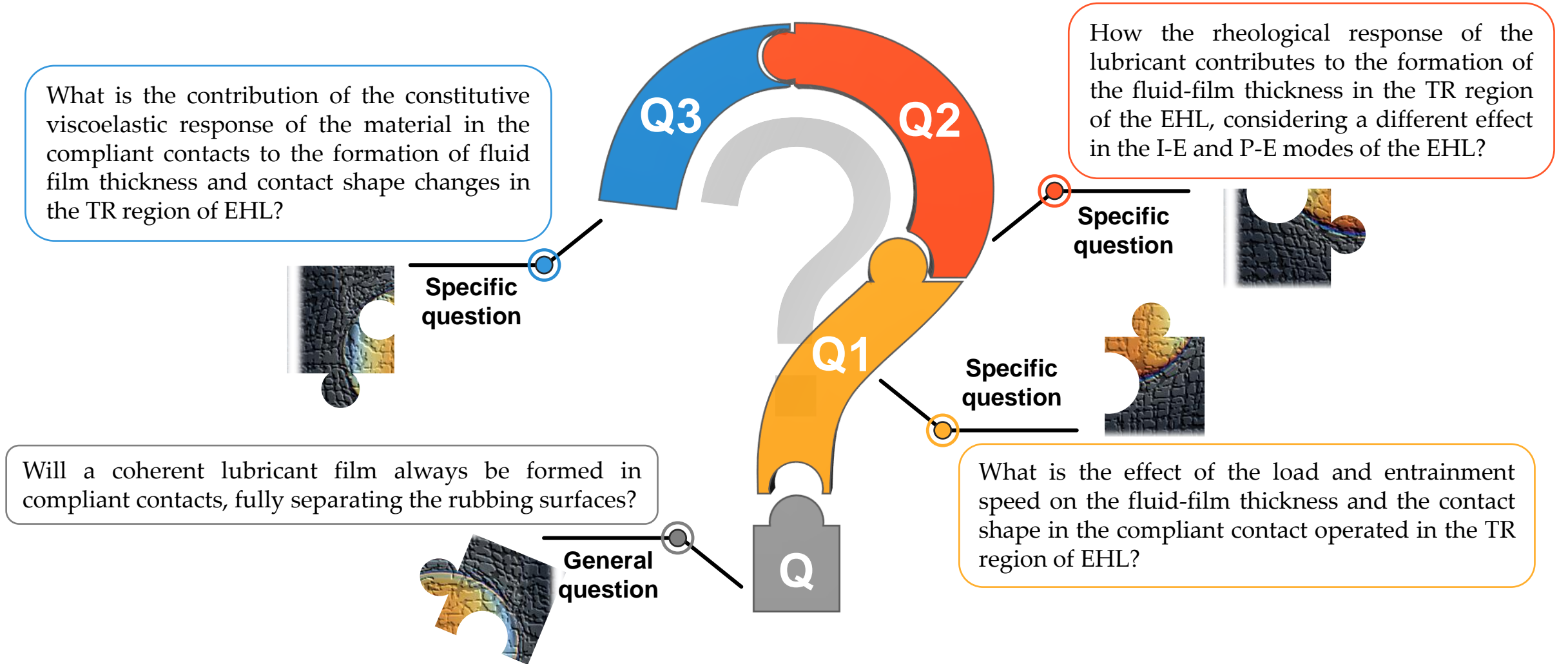
The main aim is to clarify the tribological behavior of the compliant contacts operating in the TR region between the I-E and P-E modes of EHL.



## Sub-aims



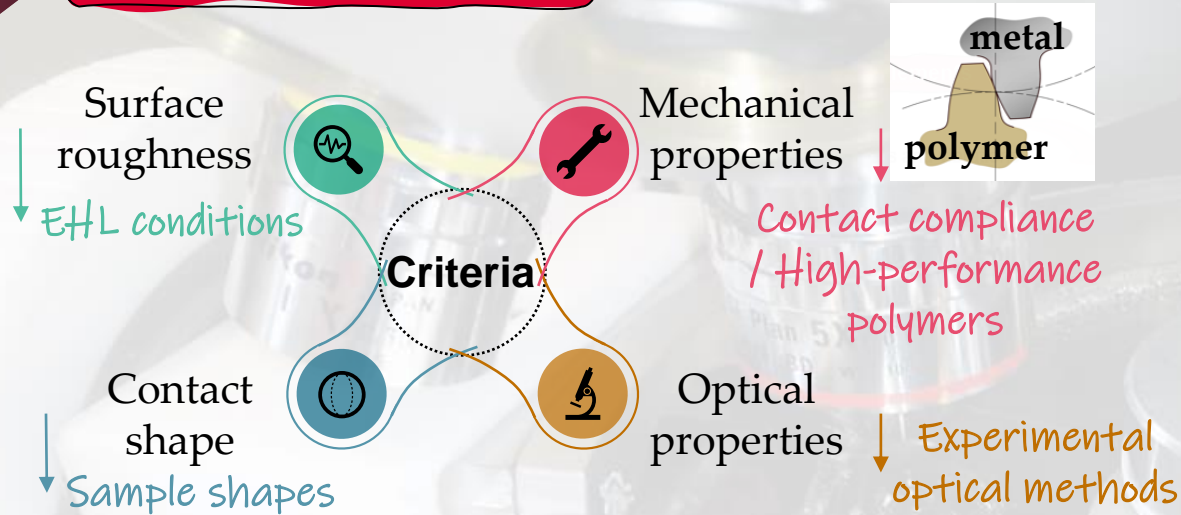
# OVERVIEW OF SCIENTIFIC QUESTIONS





# MATERIALS AND METHODS

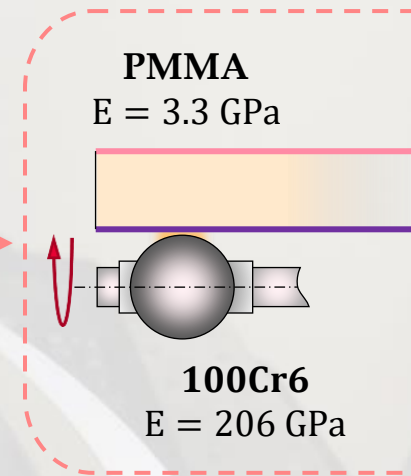
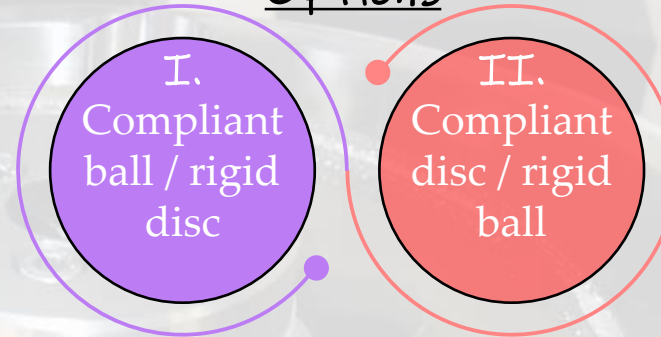
## Selection of materials



## Simulation of compliant contact

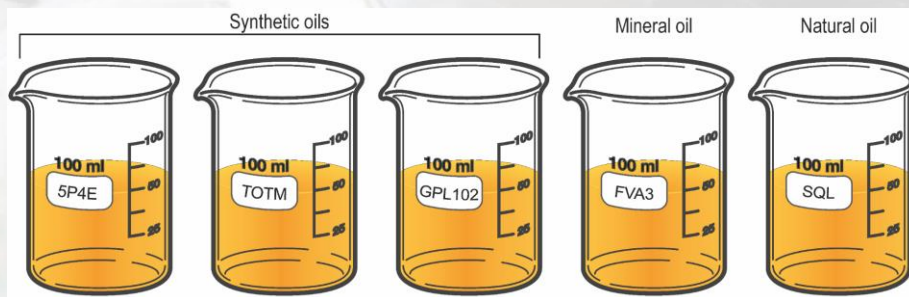
- Amorphous or semi-crystalline polymer
- Circular contact shape

### Options



## Selection of lubricants

- Reference mineral, synthetic and natural lubricants (5P4E, TOTM)
- Wide viscosity interval



## Overview of experimental conditions

Property	Interval / Value
Entrainment speed, $U_E$ (m/s)	$10^{-4}$ – $10^1$
Normal load, $W$ (N)	5 – 100
Temperature, $T$ ( $^{\circ}\text{C}$ )	22 – 130
Dynamic viscosity at $40^{\circ}\text{C}$ , $\eta$ (Pa s)	0.0157 – 0.37
Pressure-viscosity coefficient at $40^{\circ}\text{C}$ , $\alpha$ ( $\text{GPa}^{-1}$ )	18.1 – 37.0
Sliding-rolling ratio, SRR	-1 – 1
Ellipticity, $k$	1

# MATERIALS AND METHODS

## Experimental equipment

### Surface texture analysis

Bruker 3D optical profilometer



### Rheological analysis of lubricants

HAAKE RotoVisco1 viscometer



### Rheological analysis of lubricants

HPV viscometer (BUT, Czech Republic)



### Lubricant film analysis

Rotational optical tribometer (BUT, Czech Republic)



### DMA analysis

DMA1 dynamic mechanical analyzer



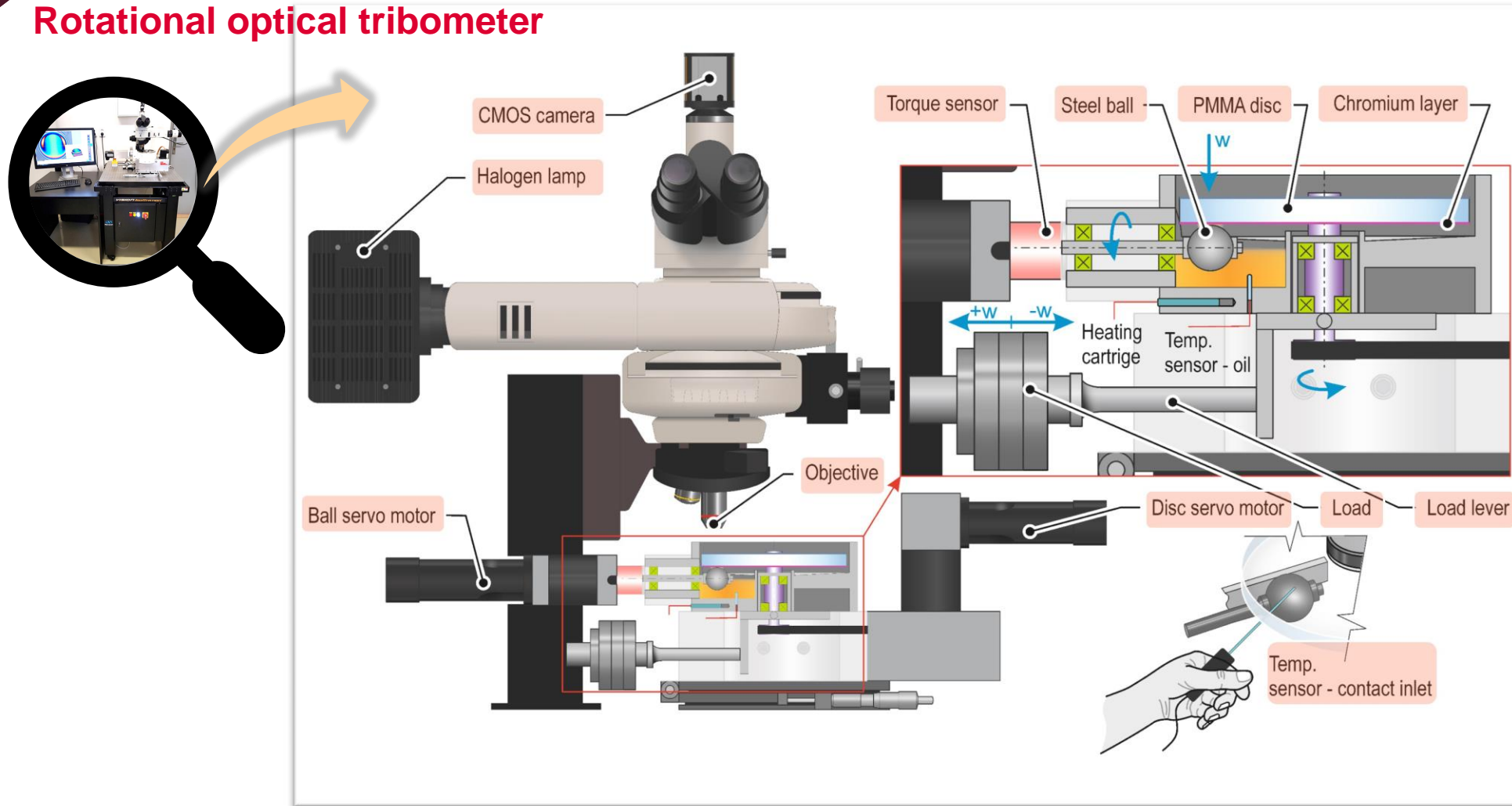
### Nano-DMA analysis

Hysitron TI Premier Nanoindenter



# MATERIALS AND METHODS

## Rotational optical tribometer



# RESULTS AND DISCUSSION



What is the effect of the load and entrainment speed on the fluid-film thickness and the contact shape in the compliant contact operated in the TR region of EHL?

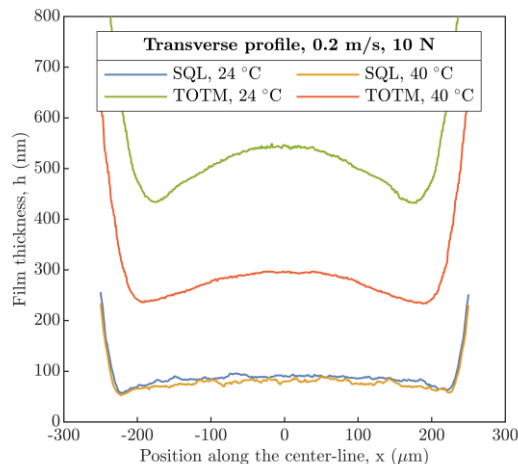
## Load effect – below $T_g$

H1.a

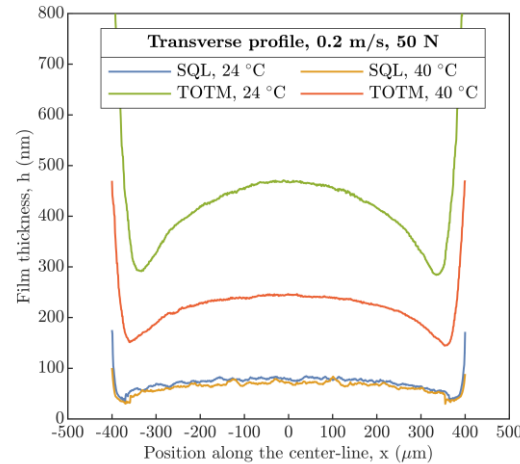
“The effect of load will be significantly dependent on the operating temperature below  $T_g$ , where the load-dependent behavior of the film thickness will be manifested.”



## Film shape – transverse profiles

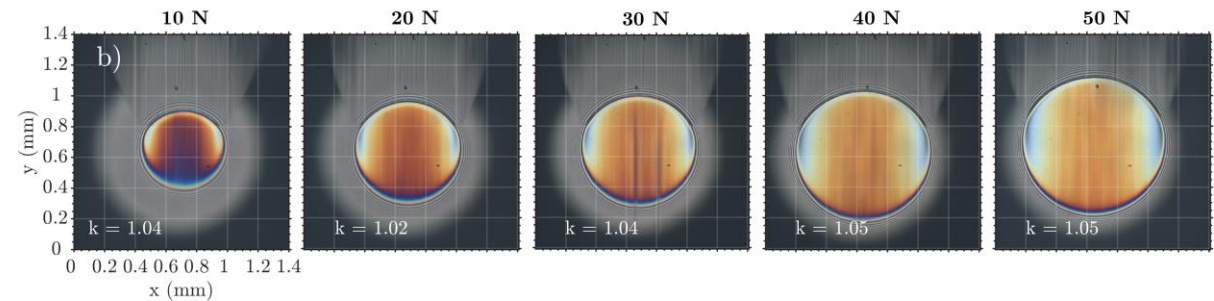


10 N



50 N

## Ellipticity and contact area



- Load transmitted directly through the fluid → no interaction between surface asperities,
- Significant reduction in lubricant film as a function of load,
- $\Delta$  between central and minimum lubricant film gradually increases with magnitude of load,
- Only slight increase in ellipticity with magnitude of load.

# RESULTS AND DISCUSSION



What is the effect of the load and entrainment speed on the fluid-film thickness and the contact shape in the compliant contact operated in the TR region of EHL?

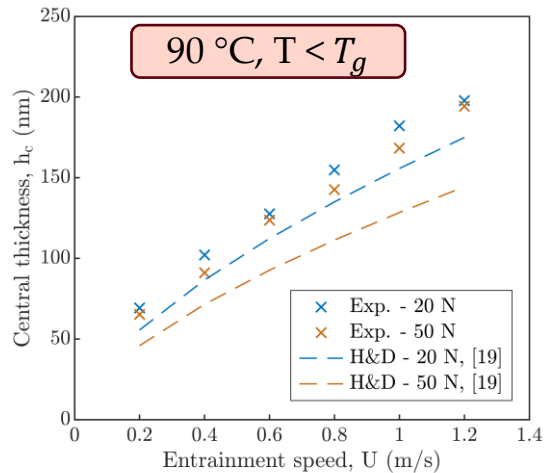
## Load effect – above $T_g$ (PMMA $T_g \sim 105^\circ\text{C}$ )

H1.b

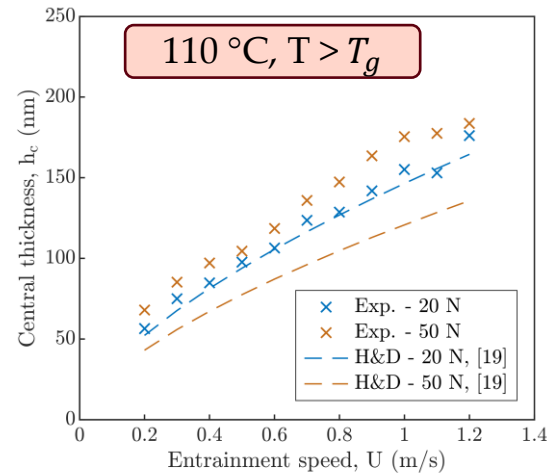
“Near and above  $T_g$ , the load-dependent behavior of the fluid-film thickness will be negligible although a significant increase in the contact area and asymmetric deformation of the contact shape will be exhibited.”



### Central film thickness

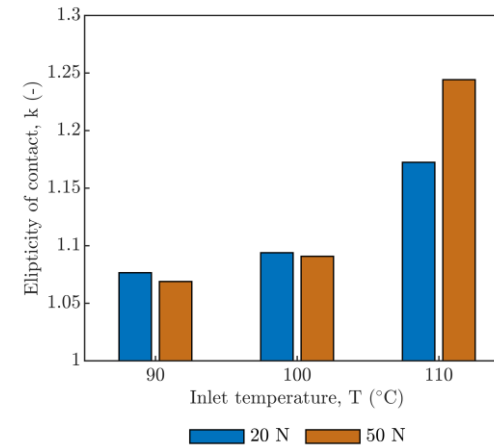


(a)

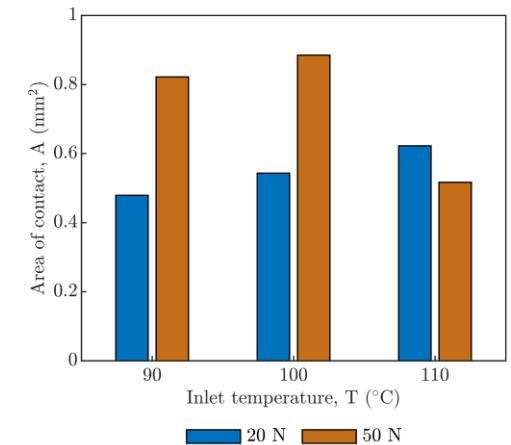


(b)

### Ellipticity



### Contact area



- Above  $T_g$ , the lubricant film surprisingly increase as a function of load,
- Above  $T_g$ , significant increase in ellipticity with load  $\rightarrow$  change of contact shape from circular to elliptical,
- Below  $T_g$ , contact area gradually increase with load up to  $T_g$ . Above  $T_g$ , opposite effect discovered.

# RESULTS AND DISCUSSION



What is the effect of the load and entrainment speed on the fluid-film thickness and the contact shape in the compliant contact operated in the TR region of EHL?

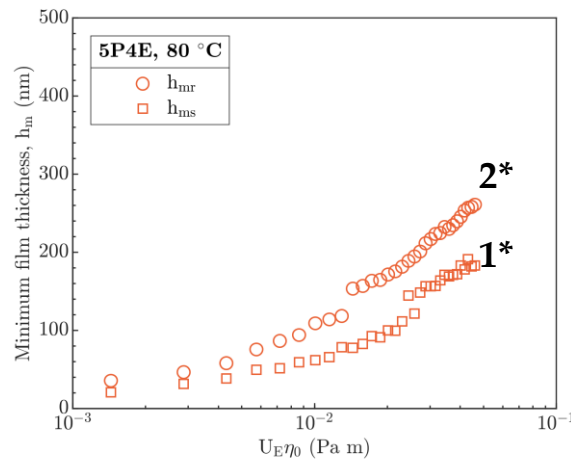
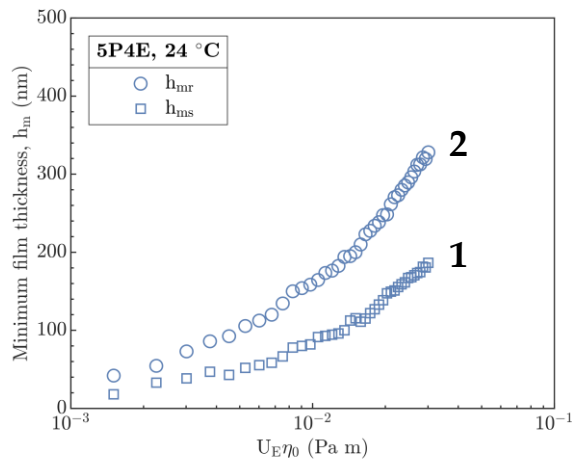
## Entrainment speed effect

H1.c

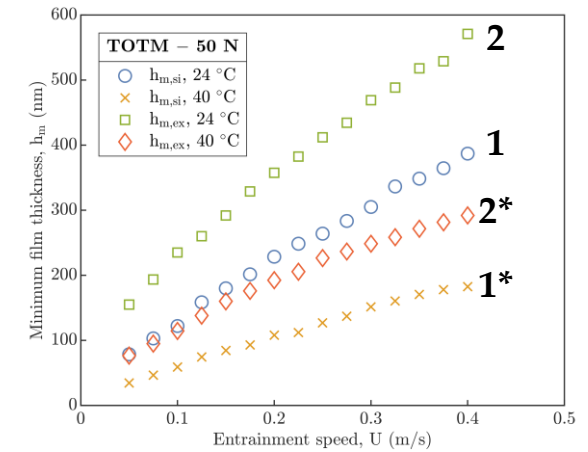
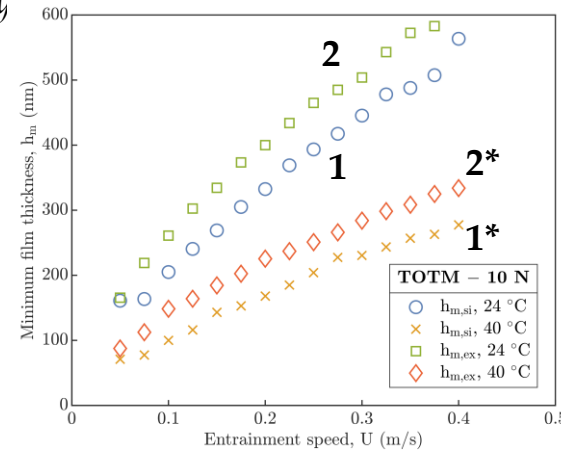
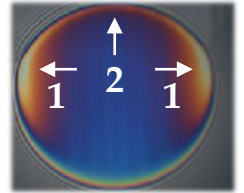
“The increase of the entrainment speed will cause a transition of minimum film thickness from the side lobes to the exit of the contact. However, the shape of the compliant contact will be only slightly affected.”



## Minimum film thickness – 5P4E

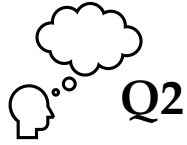


## Minimum film thickness – TOTM



- $\Delta$  between the film thickness at the side lobes and at the exit from the contact gradually increased with  $U_e$ ,
- No transition of minimum film thickness as a function of  $U_e \rightarrow$  minimum at the side lobes.

# RESULTS AND DISCUSSION



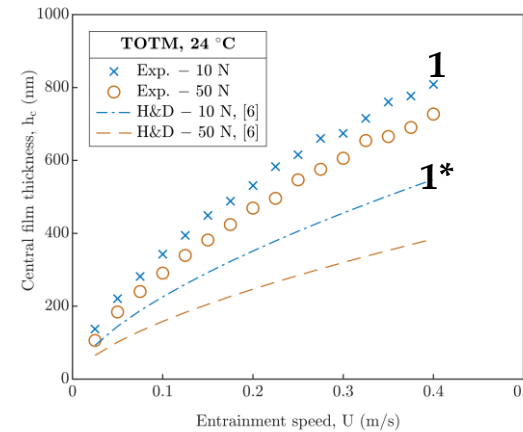
How the rheological response of the lubricant contributes to the formation of the fluid-film thickness in the TR region of the EHL, considering a different effect in the I-E and P-E modes of the EHL?

## Pressure-viscosity effect

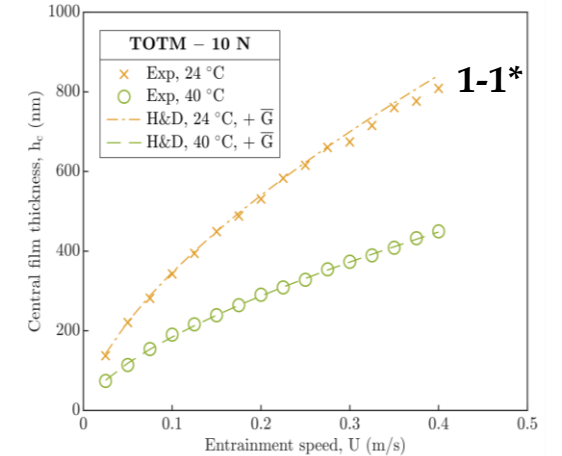


"In accordance with the EHL theory, the pressure-viscosity response of the lubricant to the formation of the fluid film thickness is usually neglected in the I-E mode of EHL. However, this effect will be more significant in the TR region than in the I-E mode."

hc – H&D I-E



hc – H&D I-E +  $\bar{G}$



TOTM

Rheological exp.

$\eta - p$

PV coef.  $\alpha$

$$\bar{G} = E' \alpha$$

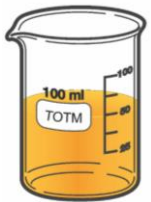
Film thickness exp.

Data regression

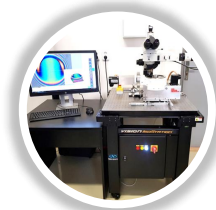
H&D I-E +  $\bar{G}$

- P-E  $\rightarrow x = 0.53$
- I-E  $\rightarrow x = 0$
- TR  $\rightarrow x = ?$

$$H_c = 7.32 (1 - 0.72 e^{-0.28k}) \bar{U}^{0.64} \bar{W}^{-0.22} \bar{G}^{0.085}$$

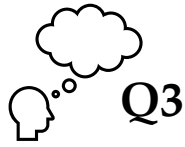


(measured by Ing. Polnicky)

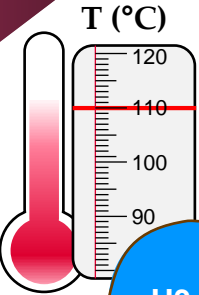


$h_c$

# RESULTS AND DISCUSSION



What is the contribution of the constitutive viscoelastic response of the material in the compliant contacts to the formation of fluid film thickness and contact shape changes in the TR region of EHL?



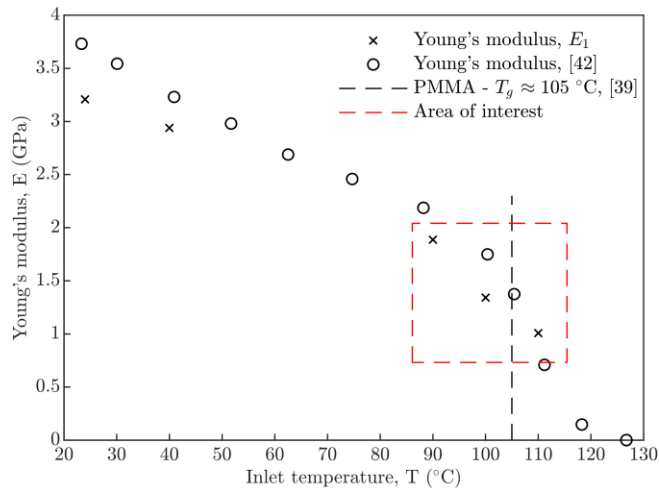
## Temperature effect

H3.a

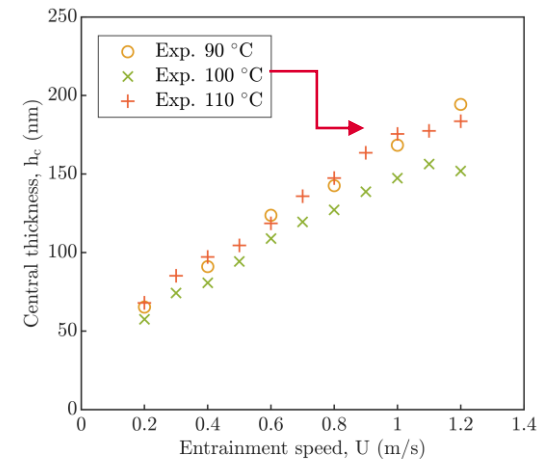
"The increase in temperature will cause a significant decrease in material stiffness, and, consequently, in terms of the EHL theory, a shift from the TR region to the I-E mode of EHL, which will take effect by increasing the fluid-film thickness in the compliant contact."



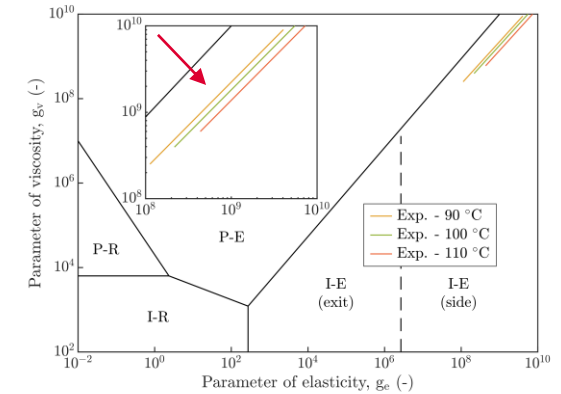
## Elastic modulus of PMMA vs temperature



## Central film thickness



## Validation of EHL mode



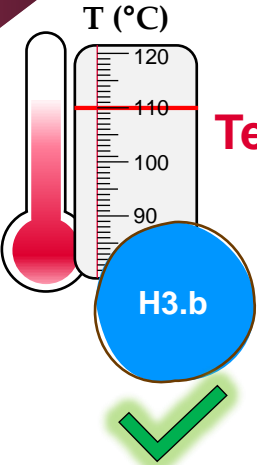
- Above  $T_g$ , increase of central thickness with temperature was discovered despite lubricant viscosity decrease  $\rightarrow$  contact softening,
- Shift of contact operation region from TR to I-E mode of EHL as a function of temperature.



# RESULTS AND DISCUSSION



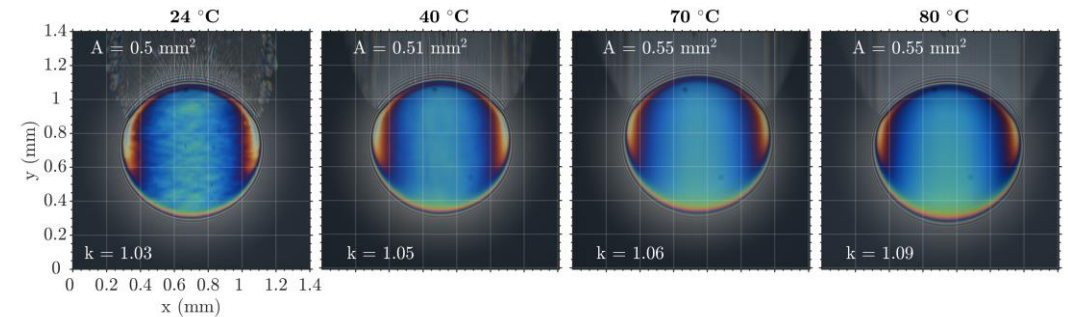
What is the contribution of the constitutive viscoelastic response of the material in the compliant contacts to the formation of fluid film thickness and contact shape changes in the TR region of EHL?



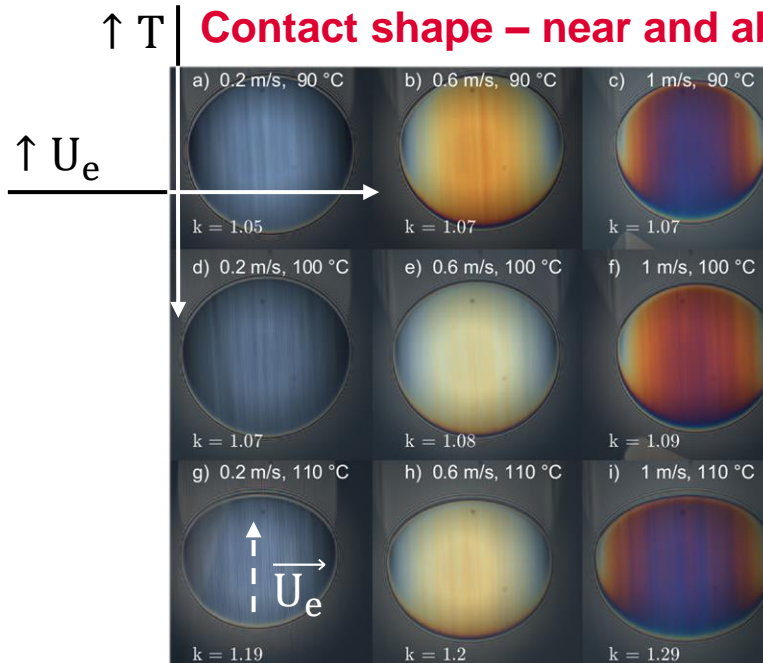
## Temperature effect

*“The temperature effect will be more critical for the conformational viscoelastic changes in the internal polymer structure influencing the contact shape rather than for possible defects by forming an unstable lubricant film and even above the  $T_g$  of solid material.”*

## Contact shape – below $T_g$



## Contact shape – near and above $T_g$



- Anisotropic deformation of the contact with  $T$  prevalent in direction perpendicular to  $U_e$ ,
- Running contact always dimensionally smaller relative to static contact,
- Below  $T_g$ , ellipticity of contact almost unchanged relative to the  $T$  and  $U_e$ ,
- Above  $T_g \rightarrow$  fully flooded conditions without film thickness defects,

# RESULTS AND DISCUSSION

## Viscoelasticity effect



*“An increase in the loading frequency of the solid material, referred to as the entrainment speed in the EHL, will make the compliant contact much stiffer, resulting in a decrease in the fluid-film thickness, although this effect will weaken with increasing temperature.”*

### Analysis of viscoelastic properties

- Nano-DMA experiments
- $E^*$ ,  $E'$ ,  $E''$  and  $\tan \delta$  parameters
- Time-temperature superposition
- Generalized Maxwell model
- Relaxation modulus  $E_r$

### Analysis of film thickness

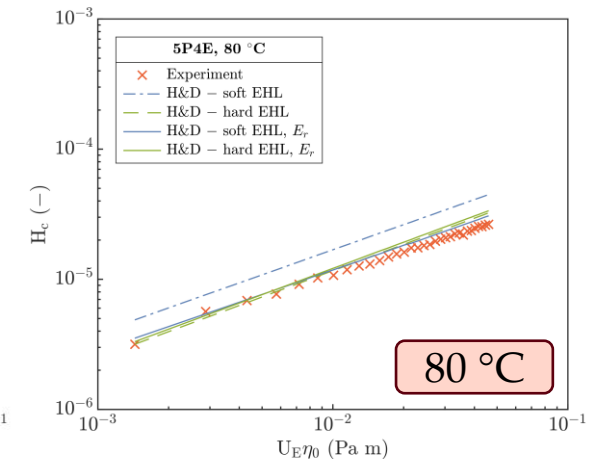
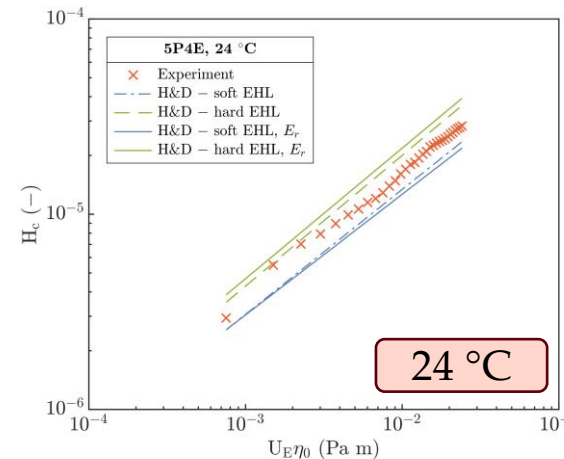
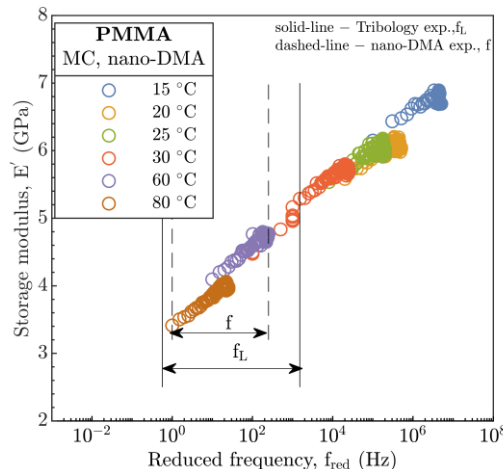
#### H&D – I-E and P-E models (substitution $E_r$ )

$$H_c = 7.32 (1 - 0.72 e^{-0.28k}) \bar{U}^{0.64} \bar{W}^{-0.22}$$

$$H_c = 2.69 (1 - 0.61 e^{-0.73k}) \bar{U}^{0.67} \bar{W}^{-0.067} \bar{G}^{0.53}$$

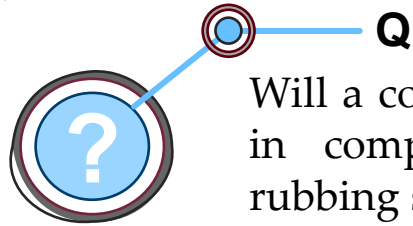
#### Experimental data vs H&D models

#### Time-temperature superposition



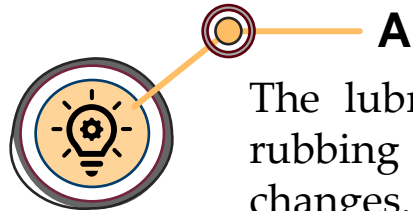
# CONCLUSION

## General question Q



Q

Will a coherent lubricant film always be formed in compliant contacts, fully separating the rubbing surfaces?



A

The lubricant film always fully separated the rubbing surfaces despite the contact shape changes.

Impacted research papers 3 x



## Main contributions of the thesis



Identification of **fluid-film thickness** and **contact shape** changes in compliant contacts operating in the **TR region** of EHL.



Implementation of the experimentally obtained **viscoelastic response** of the solid material and the **rheological response** of the lubricant into the **EHL models**.



Experimental investigation of the film thickness in compliant EHL contacts operated near the **glass-transition temperature** by the **optical interferometry method**.

# CONCLUSION

## Journal papers with IF

- A**
- **KRUPKA, Jiri**, DOCKAL, Krystof, KRUPKA, Ivan and HARTL, Martin. Elastohydrodynamic Lubrication of Compliant Circular Contacts near Glass-Transition Temperature. *Lubricants* [online]. 13 July 2022. Vol. 10, no. 7, p. 155. DOI: 10.3390/lubricants10070155 (**PAPER A, IF = 3.5, Q2, Author's contribution 75 %**)



*lubricants*

2022

- B**
- **KRUPKA, Jiri**, DOCKAL, Krystof, KRUPKA, Ivan and HARTL, Martin. Polymer Lubrication: Pressure–Viscosity–Temperature Dependence of Film Thickness for Highly Loaded Compliant Contacts in Elastohydrodynamic Lubrication Regime. *Journal of Tribology* [online]. 1 February 2023. Vol. 145, no. 2. DOI: 10.1115/1.4055558 (**PAPER B, IF = 2.5, Q3, Author's contribution 75 %**)



2022

- C**
- **KRUPKA, Jiri**, DOCKAL, Krystof, SEDLACEK, Tomas, REBENDA, David, KRUPKA, Ivan and HARTL, Martin. Viscoelastic Response of Elastohydrodynamically Lubricated Compliant Contacts below Glass-Transition Temperature. *Polymers* [online]. 30 May 2023. Vol. 15, no. 11, p. 2528. DOI: 10.3390/polym15112528 (**PAPER C, IF = 5.0, Q1, Author's contribution 62 %**)



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